

**Exercise Sheet 9**  
**CS 2210 Logic for Computer Scientists (Hitzler)**  
**Solutions due: Thursday March 19, 2015, 11am**

**Exercise 46** Show Theorem 2.6.8 part 2.

Hint: This needs less than two lines: try to reduce it to part 1 of the theorem.

**Exercise 47 (no hand-in)** For any formula  $F$ , let  $F'$  be the formula obtained from  $F$  by replacing all  $\vee$  by  $\wedge$ , and by replacing all  $\wedge$  by  $\vee$ . Furthermore, let  $\overline{F}$  be obtained from  $F$  by replacing each occurrence of an atomic formula  $A$  in  $F$  by  $\neg A$ .

Example: For  $F = (A \wedge B) \vee \neg C$ , we have  $F' = (A \vee B) \wedge \neg C$  and  $\overline{F} = (\neg A \wedge \neg B) \vee \neg\neg C$ ; and  $\overline{F'} = (\neg A \vee \neg B) \wedge \neg\neg C$ .

Show by structural induction:  $F \equiv \neg\overline{F'}$  for each formula  $F$ .